

QuickCheck is a framework for automatic program testing:

- Allows to test whether the program satisfies given **properties** on **randomly generated** inputs.
- originally for Haskell, but now also for Erlang, Scala, Java, etc.
- The library has:
 - combinators for describing properties which functions should satisfy;
 - generators of random values for standard types;
 - combinators for constructing generators for user defined datatypes.

Basic interface

```
import Test.QuickCheck  
  
quickCheck :: Testable prop => prop -> IO ()
```

- Function `quickCheck` gets a **property** as an argument which is tested on randomly generated inputs.
- By default 100 times (but this is configurable).
- If some tests fail it outputs a counter example.

Example

Properties of `reverse`

$$\forall z. \text{reverse} (\text{reverse } z) = z$$

```
prop_RevRev      :: [Int] -> Bool
prop_RevRev xs  = reverse (reverse xs) == xs
```

$$\forall a. \forall b. \text{reverse} (a ++ b) = (\text{reverse } b) ++ (\text{reverse } a)$$

```
prop_RevApp      :: [Int] -> [Int] -> Bool
prop_RevApp xs ys = reverse (xs ++ ys)
                  == reverse ys ++ reverse xs
```

Example

Properties of `reverse`

$$\forall Z. \text{reverse} (\text{reverse } Z) = Z$$

Let's try it out ...

```
pr | Main> quickCheck prop_RevRev
pr | +++ OK, passed 100 tests.

   | Main> quickCheck prop_RevApp
   | +++ OK, passed 100 tests.
```

```
prop_RevApp      :: [Int] -> [Int] -> Bool
prop_RevApp xs ys = reverse (xs ++ ys)
                  == reverse ys ++ reverse xs
```

Example (cont.)

Properties of `reverse`

$$\forall a. \forall b. \text{reverse } (a ++ b) = (\text{reverse } b) ++ (\text{reverse } a)$$

```
prop_RevApp      :: [Int] -> [Int] -> Bool
prop_RevApp xs ys = reverse (xs ++ ys)
                  == reverse ys ++ reverse xs
```

$$\forall a. \forall b. \text{reverse } (a ++ b) = (\text{reverse } a) ++ (\text{reverse } b)$$

```
prop_RevWrong   :: [Int] -> [Int] -> Bool
prop_RevWrong xs ys = reverse (xs ++ ys)
                    == reverse xs ++ reverse ys
```

Example (cont.)

Properties of `reverse`

$$\forall a. \forall b. \text{reverse } (a ++ b) = (\text{reverse } b) ++ (\text{reverse } a)$$

Let's try it out ...

```

Main> quickCheck prop_RevWrong
*** Failed! Falsifiable (after 3 tests and 2 shrinks):
 [0]
 [1]

```

```

prop_RevWrong :: [Int] -> [Int] -> Bool
prop_RevWrong xs ys = reverse (xs ++ ys)
                    == reverse xs ++ reverse ys

```

Properties

```
class Testable prop where
  property :: prop -> Property
```

```
instance Testable Bool
```

```
instance (Arbitrary a, Show a, Testable prop) =>
  Testable (a -> prop)
```

- Properties are expressions which type belongs to class `Testable`.
- Arguments should be of a monomorphic type.
 - Necessary for knowing how to generate arguments.
- Naming convention: prefix `prop_`

Properties

Example: insertion sort

```
isort :: Ord a => [a] -> [a]
```

```
isort = foldr insert []
```

```
insert :: Ord a => a -> [a] -> [a]
```

```
insert x [] = [x]
```

```
insert x (y:ys) | x <= y = x : y : ys
```

```
                | otherwise = y : insert x ys
```


Properties

Sorting property 1: sorted list must be ordered

```
prop_sortOrder :: [Int] -> Bool
```

```
prop_sortOrder xs = ordered (isort xs)
```

```
ordered :: Ord a => [a] -> Bool
```

```
ordered (x:y:ys) = x <= y && ordered (y:ys)
```

```
ordered ys      = True
```

Properties

Sorting property 2: sorted and original list have same elements

```
prop_sortElems :: [Int] -> Bool
```

```
prop_sortElems xs = sameElems xs (isort xs)
```

```
sameElems :: Eq a => [a] -> [a] -> Bool
```

```
sameElems xs ys = null (xs \\ ys) && null (ys \\ xs)
```

Properties

Inspecting test data

```
collect :: (Show a, Testable prop) => a -> prop -> Property
```

- Function `collect` gathers statistics about test cases.
- This information is displayed when a test passes.

Properties

How many test cases were non-empty?

```
Main> let p = prop_sortOrder
Main> quickCheck (\ xs -> collect (null xs) (p xs))
+++ OK, passed 100 tests.
93% False
 7% True
```

Properties

How long were argument lists?

```
Main> let 120 xs = length xs `div` 20
Main> quickCheck (\xs -> collect (120 xs) (p xs) == 100)
+++ OK, passed 100 tests:
53% 0
22% 1
14% 2
 7% 3
 4% 4
```

Properties

I What were actual arguments?

```
Main> quickCheck (\ xs -> collect xs (p xs))
+++ OK, passed 100 tests:
 8% []
 1% [97723, 95805, -104521, 45943, -73844, 6249, 64936]
...
```

Properties

Insertion property: insertion preserves sorting
(ver. 1)

```
prop_insertOrder1      :: Int -> [Int] -> Bool
prop_insertOrder1 x xs = ordered xs `implies`
                          ordered (insert x xs)
```

```
implies      :: Bool -> Bool -> Bool
implies x y = not x || y
```

Properties

Insertion property: insertion preserves sorting

Problem!

```
Main> let p = prop_insertOrder1
Main> quickCheck(\x xs -> collect (ordered xs) (p x xs))
+++ OK, passed 100 tests:
87% False
13% True
```

implies $x \ y = \text{not } x \ || \ y$

Properties

Implications

```
(==>) :: Testable prop => Bool -> prop -> Property
```

```
instance Testable Property
```

- The combinator `(==>)` ignores inputs where premise is not satisfied and regenerates new test data.
- By default 500 times (but this is configurable).

Properties

Insertion property: insertion preserves sorting
(ver. 2)

```
prop_insertOrder2      :: Int -> [Int] -> Property
prop_insertOrder2 x xs = ordered xs ==>
                          ordered (insert x xs)
```

Properties

Insertion property: insertion preserves sorting

Better but still ...

```
Main> let p = prop_insertOrder2
Main> quickCheck(\x xs -> collect(ordered xs)(p x xs))
*** Gave up! Passed only 82 tests (100% True).
```

Properties

Universal quantification

```
forall :: (Show a, Testable prop) =>  
         Gen a -> (a -> prop) -> Property
```

- The combinator `forall` gets an explicit generator which is used for generating test cases.
- Allows to use special generators which guarantee that input satisfies certain properties.

Properties

Insertion property: insertion preserves sorting
(ver. 3)

```
prop_insertOrder3    :: Int -> Property
prop_insertOrder3 x = forAll orderedList (\ xs ->
                                ordered (insert x xs))
```

Properties

In **Now works!!**

(v
pr
pr

```
Main> quickCheck (forall orderedList ordered)
+++ OK, passed 100 tests.
Main> quickCheck prop_insertOrder3
+++ OK, passed 100 tests.
```

(s))

Generators

Generators

```
newtype Gen a = ...
```

```
instance Monad Gen
```

```
instance Functor Gen
```

```
instance (Testable prop) => Testable (Gen prop)
```

- Generators belong to an abstract data type `Gen`.
- `Gen` is a monad which effect is "access" to random numbers.

Generators

Sampling generated data

```
sample :: Show a => Gen a -> IO ()
```

Combinators for generators

```
choose      :: Random a => (a, a) -> Gen a  
elements   :: [a] -> Gen a  
oneof      :: [Gen a] -> Gen a  
frequency  :: [(Int, Gen a)] -> Gen a  
sized      :: (Int -> Gen a) -> Gen a  
vectorOf   :: Int -> Gen a -> Gen [a]
```


Generators

Default generators

```
class Arbitrary a where  
  arbitrary :: Gen a  
  shrink    :: a -> [a]  
  
shrink _ = []
```

- Types belonging to the class `Arbitrary` have the default generator.
- In addition, the class has a method `shrink` which is used for generating smaller counterexamples:
 - `shrink` returns a list of structurally smaller values;
 - if the property fails it is retested on values returned by `shrink` until there is no smaller counterexamples.

Generators

Simple generators

```
instance Arbitrary Bool where
  arbitrary = choose (False, True)
```

```
instance (Arbitrary a, Arbitrary b) => Arbitrary (a,b) where
  arbitrary = liftM2 (,) arbitrary arbitrary
```

```
data Color = Red | Blue | Green
```

```
instance Arbitrary Color where
  arbitrary = elements [Red, Blue, Green]
```

Generators

Simple generators

```
instance Arbitrary a => Arbitrary (Maybe a) where
  arbitrary = oneof [ return Nothing
                    , liftM Just arbitrary]
```

Generators

Simple generators

```
instance Arbitrary a => Arbitrary (Maybe a) where  
  arbitrary = oneof [ return Nothing
```

Problem!

Half of the values are Nothing!!

Generators

Simple generators

```
instance Arbitrary a => Arbitrary (Maybe a) where
  arbitrary = oneof [ return Nothing
                    , liftM Just arbitrary]
```

A better version

```
instance Arbitrary a => Arbitrary (Maybe a) where
  arbitrary = frequency [ (1, return Nothing)
                        , (3, liftM Just arbitrary)]
```

Generators

Generating integers (ver. 1)

```
instance Arbitrary Int where  
  arbitrary = choose (-20, 20)
```

Generators

Generating integers (ver. 1)

```
instance Arbitrary Int where  
  arbitrary = choose (-20, 20)
```

Generating integers (ver. 2)

```
instance Arbitrary Int where  
  arbitrary = sized (\ n -> choose (-n, n))
```

Generators

Generating recursive data types (ver. 1)

```
data Tree a = Leaf a
           | Node (Tree a) (Tree a)
```

```
instance Arbitrary a => Arbitrary (Tree a) where
  arbitrary = frequency [(1, liftM Leaf arbitrary)
                        , (2, liftM2 Node arbitrary arbitrary)]
```


Generators

Generating recursive data types (ver. 1)

```
data Tree a = Leaf a
```

Problem!

```
instance MonadTree Tree where  
  arbitrary = frequency [(1, liftM Leaf arbitrary)  
                        , (2, liftM2 Node arbitrary arbitrary)]
```

Termination is not guaranteed!!

Generators

Generating recursive data types (ver. 2)

```
instance Arbitrary a => Arbitrary (Tree a) where
  arbitrary = sized arbitraryTree

arbitraryTree    :: Arbitrary a => Int -> Gen (Tree a)
arbitraryTree 0 = liftM Leaf arbitrary
arbitraryTree n = frequency [ (1, liftM Leaf arbitrary)
                               , (4, liftM2 Node t t) ]
  where t = arbitraryTree (n `div` 2)
```

NB!

- The second equation has the possibility to generate Leaf.
- Otherwise would generate only balanced trees.

Generators

Predefined special generators

```
newtype OrderedList a = Ordered [a]  
instance (Ord a, Arbitrary a) => Arbitrary (OrderedList a)
```

```
newtype NonEmptyList a = NonEmpty [a]  
instance Arbitrary a => Arbitrary (NonEmptyList a)
```

```
newtype Positive a = Positive a  
instance (Num a, Ord a, Arbitrary a) => Arbitrary (Positive a)
```

```
newtype NonZero a = NonZero a  
newtype NonNegative a = NonNegative a
```

Function Generators

```
class CoArbitrary a where
  coarbitrary :: a -> Gen b -> Gen b

instance (CoArbitrary a, Arbitrary b) => Arbitrary (a -> b)
```

Example

```
variant :: Integral n => n -> Gen a -> Gen a

instance CoArbitrary a => CoArbitrary [a] where
  coarbitrary []      = variant 0
  coarbitrary (x:xs) = variant 1 . coarbitrary (x,xs)
```

- You should use `variant` to perturb the random generator; the goal is that different values for the first argument will lead to different calls to `variant`.

QuickCheck

Conclusion

- As Haskell is lazy language, it allows to use infinite values; but properties may inspect only a finite part of it.
- Also provides features to test monadic values (incl. IO).