Estonian Theory Days, Koke, Estonia

## Designated Verifier Signatures: Attacks, New Definitions and Constructions



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#### **Outline**

- Motivation for DVS
- Attacks on Some Previous Constructions
- New Security Notions
- Our Own Construction
- Conclusion

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#### **Motivation**

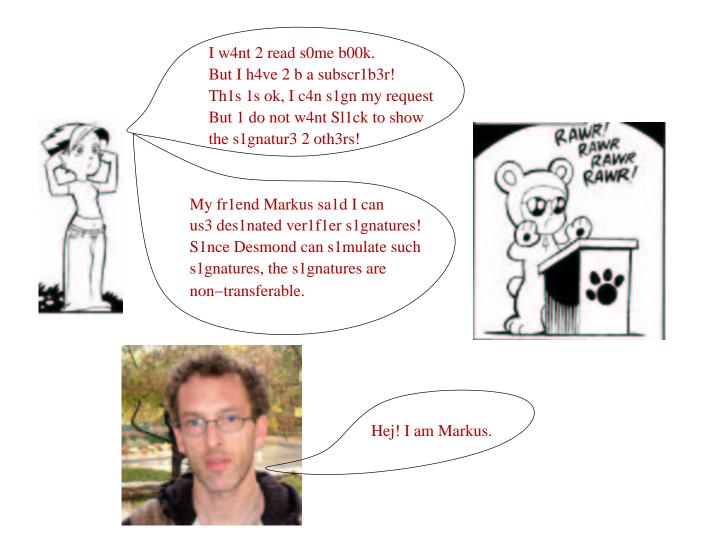
I w4nt 2 read s0me b00k. But I h4ve 2 b a subscr1b3r! Th1s 1s ok, I c4n s1gn my request But 1 do not w4nt S11ck to show the s1gnatur3 2 oth3rs!





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#### **Motivation**



#### More applications?

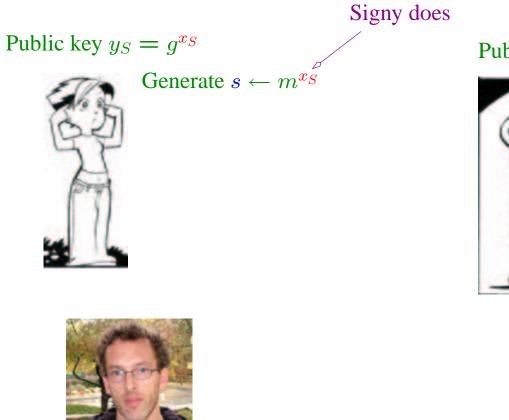
- E-voting: Signy is a voter, Desmond is a tallier. Desmond gets to know voter is Signy but cannot prove it to anybody else.
- Also related to privacy-preserving data-mining:
  - \* Desmond knows Signy is a loyal customer; Signy gets bonus
  - ★ Desmond can add information about Signy in the database and process it later
  - Desmond can't prove to anybody else that the database is correct but he trusts himself!
- Etc etc etc

Public key  $y_S = g^{x_S}$ 

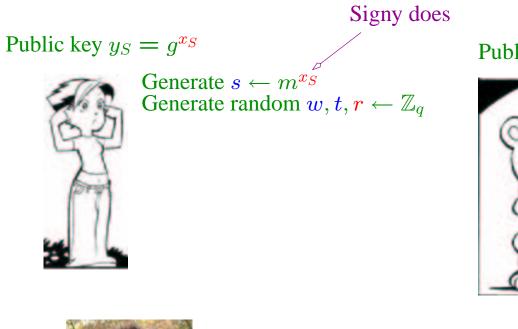
















Public key  $y_S = g^{x_S}$ 

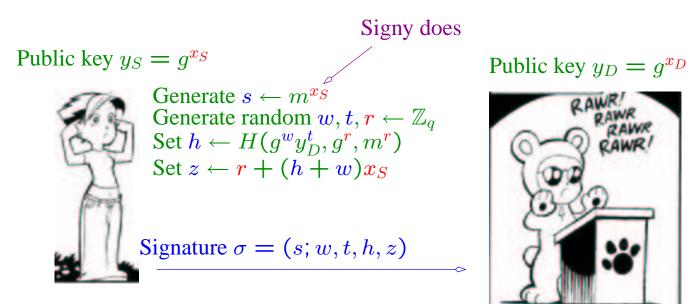


Generate  $s \leftarrow m^{x_{S}}$ Generate random  $w, t, r \leftarrow \mathbb{Z}_{q}$ Set  $h \leftarrow H(g^{w}y_{D}^{t}, g^{r}, m^{r})$ 

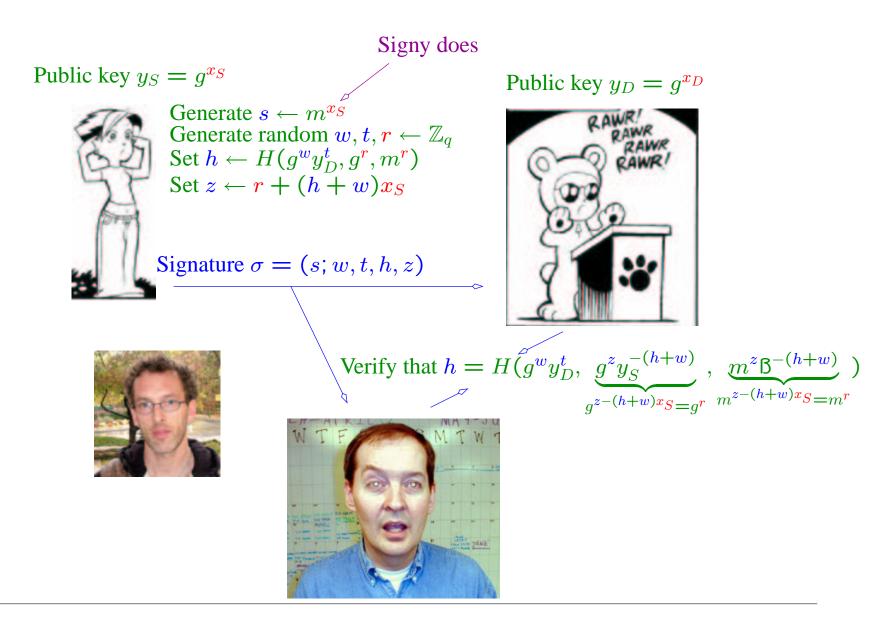
Signy does





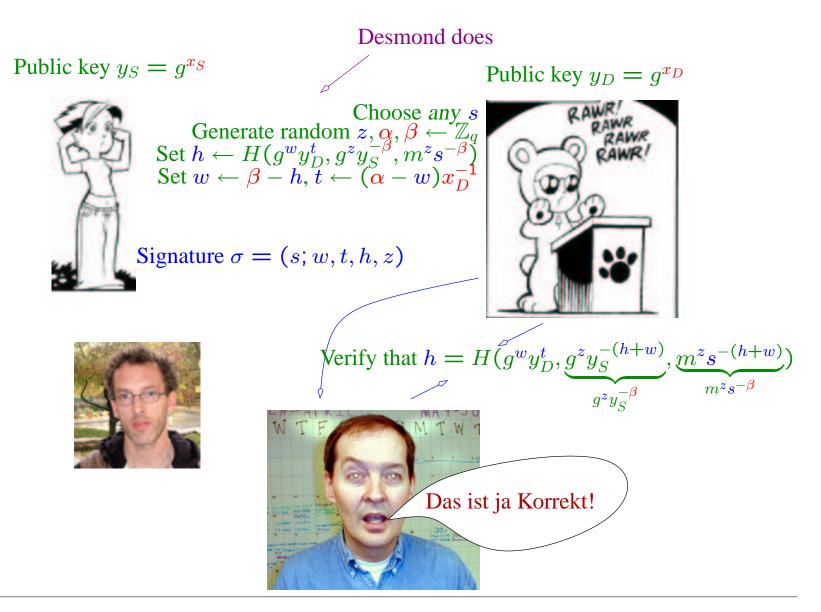






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## Thus spake Markus to Desmond:



#### Thus spake Markus to both:

• If Signy signs:  $s = m^{x_S}$ , thus  $(g, y_S, m, s)$  is a DDH tuple.

\* 
$$(g, y_S, m, s) = (g, g^a, g^b, g^{ab})$$
 for some  $a, b$ 

- Signy proves in NIZK that  $(g, y_S, m, s)$  is a DDH tuple.
- If Desmond simulates:  $\overline{s}$  is chosen randomly, thus  $(g, y_S, m, \overline{s})$  is not a DDH tuple with very high probability,  $1 \frac{1}{q}$

\*  $c = g^w y_D^t$  for which Desmond knows the trapdoor  $x_D$ 

- \* Desmond "simulates" proof by using the trapdoor for any  $\overline{s} \in \mathbb{Z}_p$
- Signy can disavow, w.h.p.  $1 \frac{1}{q}$ , by proving that  $\overline{s} \neq m^{x_s}$

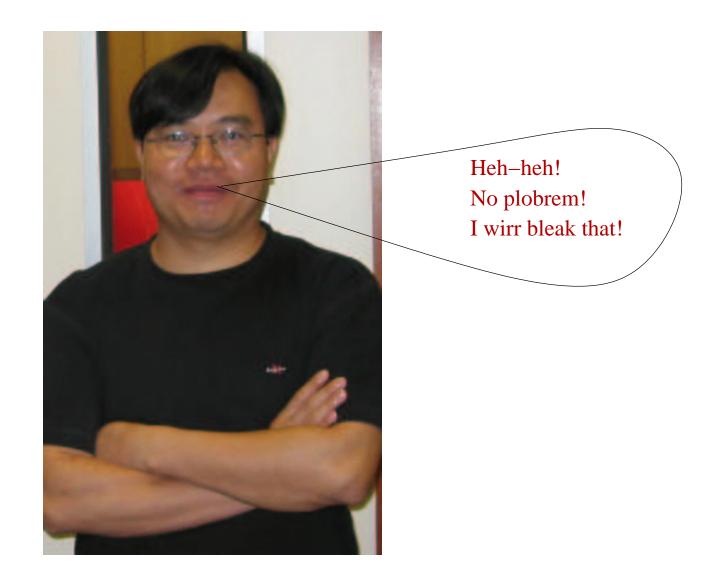
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## Thus spake Markus to both:

- To generate a valid  $\sigma \leftarrow (s; w, t, h, z)$  you must know either  $x_S$  or  $x_D$
- Thus Desmond knows  $\sigma$  was generated by Signy
  - \* Since Desmond did not generate it himself
- $\bullet$  Any third party doesn't know whether  $\sigma$  was generated by Signy or Desmond

And Signy was very happy and Desmond coverted in snow.

#### But Desmond met Guilin and Guilin spake to him:



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#### But Desmond met Guilin and Guilin spake to him:

Public key  $y_S = q^{x_S}$ Public key  $y_D = g^{x_D}$ Generate random  $w, t, r \neq \overline{r} \leftarrow \mathbb{Z}_q$ Set  $h \leftarrow H(g^w y_D^t, g^r, m^{\overline{r}})$ Set  $z \leftarrow r + (h + w)x_S$ Set  $\overline{s} \leftarrow m^{x_S} \cdot m^{(r-\overline{r})/(h+w)}$ Signature  $\sigma = (\overline{s}; w, t, h, z)$ Signy can also do this! Verify that  $h = H(g^w y_D^t, \underbrace{g^z y_S^{-(h+w)}}_{g^{z-(r-\overline{r})}=g^r}, \underbrace{m^{z}(\overline{s})^{-(h+w)}}_{m^{z-(h+w)}x_S^{-(r-\overline{r})}=m^{\overline{r}}})$ 

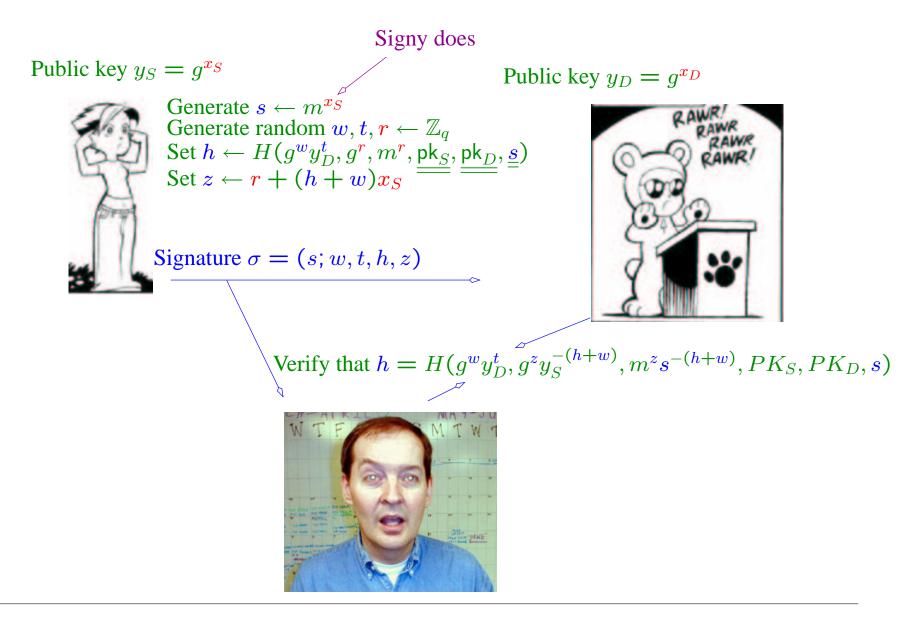
## But Desmond met Guilin and Guilin spake to him:

- Verification succeeds, thus Desmond accepts it as Signy's signature
- However, since  $\overline{s} \neq m^{x_S}$ , Signy can later disavow it!

And Desmond was not so happy anymore.



#### Quick fix:



## Then, Signy met some other people

• Steinfeld, Bull, Wang and Pieprzyk said: use a bilinear pairing  $\langle\cdot,\cdot\rangle$ 

 $\star \ \langle b^a, d^c \rangle = \langle b, d \rangle^{ac}$ 

- Signy signs m:  $s = \langle m^{x_S}, y_D \rangle = \langle m, g \rangle^{x_S x_D}$
- Desmond simulates:  $\overline{s} = \langle m^{x_D}, y_S \rangle = \langle m, g \rangle^{x_S x_D}$
- Here, Signy cannot disavow since  $s = \overline{s}$

And Signy was happy again and kissed Pieprzyk.



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## However, Desmond met Guilin again

Guilin spake to Desmond:

- Signy can compute  $y_{SD} := g^{x_S x_D}$  and publish it
- Then anybody can sign m as  ${\color{black}s}=\langle m,y_{SD}\rangle=\langle m,g\rangle^{x_Sx_D}$
- Thus Signy can delegate her subscription to your library, without revealing her public key

And Desmond wanted to cry.

## And so forth and so forth

- Signy and Desmond met many wise men who proposed better and better designated verifier signature schemes.
- However, Guilin broke them all!
- Sad story, eh?
- Signy even thought about never reading a book again!

#### What went wrong?

- [JSI1996]: disavowability claimed but does not exist
- [SBWP2003] and some other schemes were delegatable
- $\Rightarrow$  propose a modification that is *unforgeable* 
  - $\star\,$  Use as tight reductions as possible
  - $\star$  ... and as weak trust model as possible
- $\Rightarrow$  Eliminate disavowal or make it "secure"
  - Non-delegatability was never considered before
- $\Rightarrow$  Define non-delegatability and propose a non-delegatable scheme



Consider the next game:

- Choose random key pairs for Signy and Desmond
- Give the Forger both public keys, an oracle access to Signy's signing algorithm, Desmond's simulation algorithm and the hash function
- Forger returns a message m and a signature  $\sigma$

Forger is *successful* if verification on  $(m, \sigma)$  succeeds and he never asked a sign/simul query on m that returned  $\sigma$ 

Scheme is  $(\tau, q_h, q_s, \varepsilon)$ -unforgeable  $\iff$  no  $(\tau, q_h, q_s)$ -forger has success probability  $> \varepsilon$ 

Forger runs in time  $\tau$ , does  $q_h$  queries to hash function and  $q_s$  queries to either signing or simulation algorithmKoke, ETD 2005, Estonia, 26.01.2005Designated Verifier Signatures, Helger Lipmaa

#### Non-Transferability

- A scheme is *perfectly* non-transferable if signatures generated by Signy and Desmond come from the same distribution.
  - \* Perfectly non-transferable schemes *cannot* have disavowal protocols!
  - \* As we showed, JSI is perfectly non-transferable!
- A scheme is *computationally* non-transferable if signatures generated by Signy and Desmond come from distributions that are computationally indistinguishable.
  - Computationally non-transferable schemes may have a trapdoor that can be used for constructing disavowal protocols

## Non-Delegatability

Requirement: if Forger produces valid signatures with probability  $> \kappa$  then he knows either the secret key of Signy or the secret key of Desmond

We require there exists a knowledge extractor such that

If a Forger produces a valid signature σ on m w.p. ε > κ
then knowledge extractor, given (m, σ) and oracle access to Forger on the memory state that results in producing (m, σ), produces one of the two secret keys in time <sup>τ</sup>/<sub>ε-κ</sub>.

Then the scheme is  $(\tau, \kappa)$ -non-delegatable.

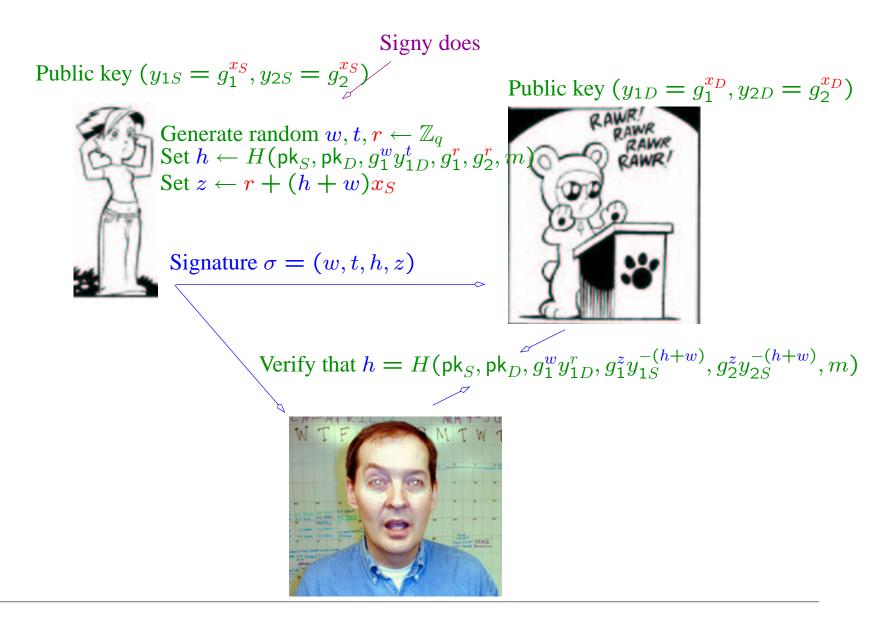
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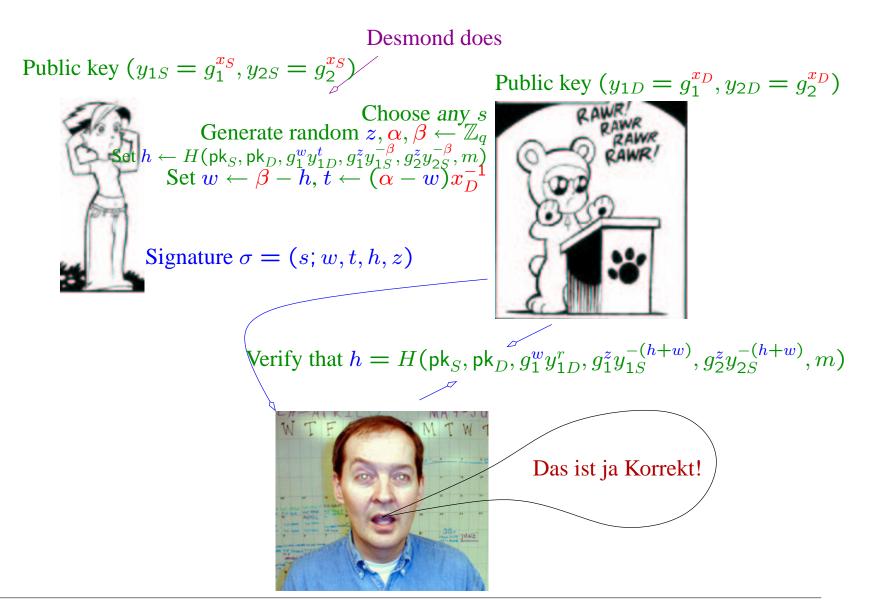
## **Underlying Idea of Our Scheme**

- If Signy signs: she proves that her public key  $(g_1, g_2, y_{1S} = g_1^{x_S}, y_{2S} = g_2^{x_S})$  is a DDH tuple.
- We again employ  $c = g^w y_D^t$  (trapdoor commitment) for which Desmond knows the trapdoor  $x_D$ , thus the proof is designated-verifier.
- Desmond simulates this proof by using the trapdoor information
- Signy cannot disavow since there is perfect non-transferability

## And Thus We Spake to Signy:



## And Thus We Spake to Desmond:



## **Properties of The New Scheme**

- Twice longer public keys than in JSI enables to get tight unforgeability reductions
  - \* In non-programmable random oracle model
- No disavowal
  - \* Orthogonal to the security requirements of an DVS scheme
- Non-delegatability: proven, but the reduction is not tight

# Unforgeability

**Theorem.** Let G, |G| = q be a  $(\tau', \varepsilon)$ -time DDH group. The proposed scheme is  $(\tau, q_h, q_s, \varepsilon)$ -unforgeable in the non-programmable random oracle model with  $\tau \leq \tau' - (3.2q_s + 5.6)t_{\text{exp}}$  and  $\varepsilon \geq \varepsilon' + q_s q_h q^{-2} + q^{-1} + q_h q^{-2}$ .

**Proof sketch:** Adversary *A* has to solve DDH on input  $(g_1, g_2, y_{1D}, y_{2D})$ . Set this to Desmond's public key, and set Signy's public key to be equal to a random DDH tuple (for which *A* knows the corresponding secret key). Give *A* an oracle access to Forger. Answer all hash queries truthfully (but store them). Answer all signing and simulation queries by following Signy's algorithm. (Possible since *A* knows Signy's secret key.) It comes out that *A* works in time and with success probability, claimed above.

**Note:** This is a tight reduction. In practical setting it means that whenever you can forge a signature—e.g.,  $2^{-80}$ —, you can almost always solve DDH and in comparable time.

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## Non-programmable random oracle model

RO model	NPRO model
Environment doesn't have access to the RO.	Environment has access to the RO.
In the Katz-Wang signature scheme: adversary does not know signer's secret key, and thus cannot create valid signa- tures without defining a $H$ that just satisfies the verification equation	In our scheme: adversary has access to Signy's secret key, and can thus create valid signatures with- out redefining <i>H</i>
<b>Best case proof</b> : shows that for every adversary, there exists a function $H$ such that the result holds	Average case proof: shows that the result holds for a randomly chosen function $H$
But $H$ depends on Forger's actions and thus cannot be instantiated in some sense!	H can be chosen in advance

## New Conventional Signature Scheme

- Take the new DVS scheme with assumption that Desmond is a trusted third party, and his public key is a common reference string (CRS).
- That is, Signy signs *m* by
  - \* Choosing random  $w, t, r \leftarrow_R \mathbb{Z}_q$
  - \* Setting  $h \leftarrow H(\mathsf{pk}_S, g_1^w y_{1S}^t, g_1^r, g_2^r, m)$
  - \* Setting  $z \leftarrow r + (h + w)x_S$  and outputting  $\sigma = (w, t, h, z)$
- New signature scheme with tight security reduction to DDH problem in NPRO+CRS model

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# Delegatability

**Theorem**. Let  $\kappa \geq 1/q$ . Assume that for some message m, Forger can produce signature in time  $\tau'$  and with probability  $\varepsilon \geq \kappa$ . Then there exists a knowledge extractor that on input a valid signature  $\sigma$  and on black-box oracle access to Forger (with an internal state compatible with  $\sigma$ ) can produce one of the two secret keys in expected time  $\tau \leq 56\tau'/\kappa$ .

**Note:** This is an imprecise reduction. For example, if Forger has advantage  $2^{-30}$  then Knowledge Extractor works in time  $2^{36} \cdot \tau'$ , with probability 1.

## **Conclusions**

- And Desmond was happy since only valid subscribers were able to borrow the books.
  - \* And these subscribers could not delegate their subscriptions!
- And Signy was happy since Desmond could not prove that she borrowed these books.

## Any questions?



Caveat: This presentation is based on a draft version of the paper!

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