# The historical role of Kharkiv in theoretical physics and the science of the cosmos

#### Manuel Hohmann

Laboratory of Theoretical Physics - Institute of Physics - University of Tartu Center of Excellence "The Dark Side of the Universe"









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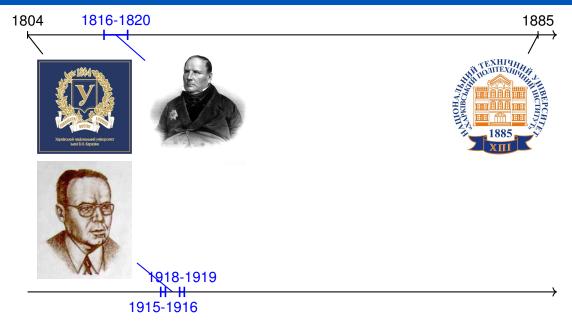
Physicum Seminar - 7. 4. 2022

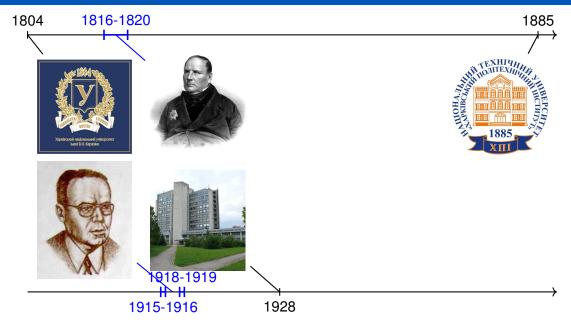
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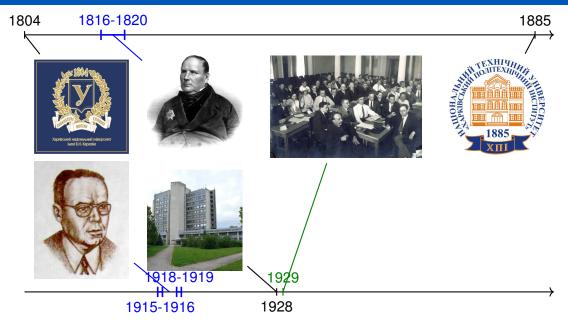


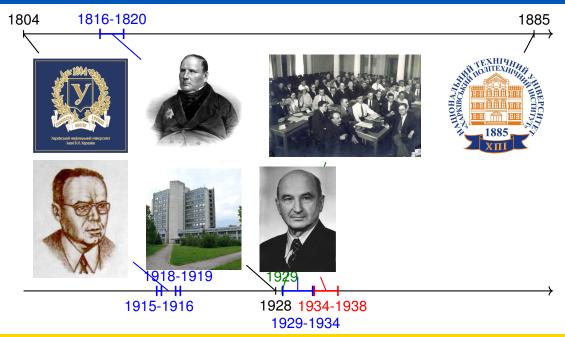


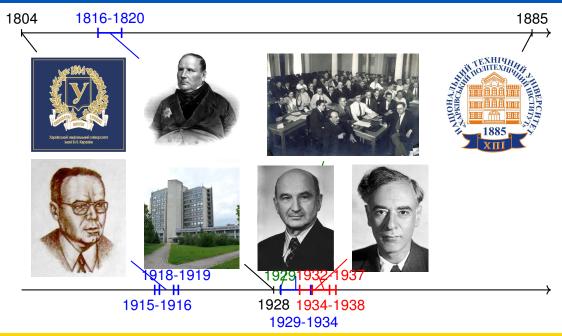






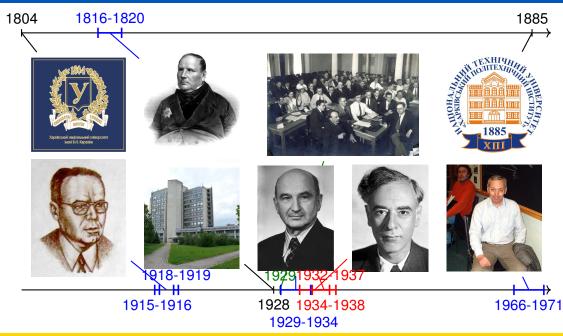




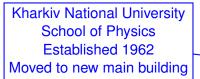


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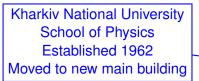
Kharkiv's role in theoretical physics













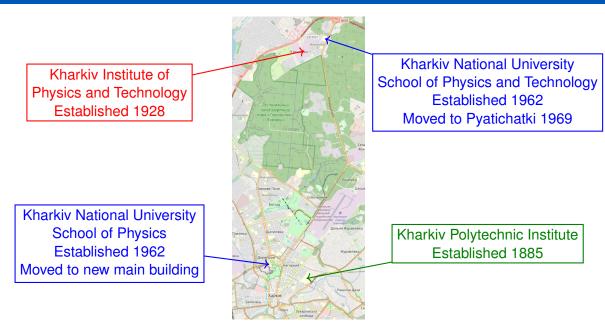
Kharkiv Polytechnic Institute Established 1885

Kharkiv National University School of Physics Established 1962 Moved to new main building



Kharkiv National University School of Physics and Technology Established 1962 Moved to Pyatichatki 1969

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# Mikhail Ostrogradsky

- \* September 24, 1801, Pashenivka; † January 1, 1862, Poltava.
- 1816-1820 studied at Kharkiv University.
- Did not receive his degree for not attending theology.
- 1822-1826 studied at Sorbonne & College de France.
- 1828 moved to Saint Petersburg.
- 1830 extraordinary member of St. Petersburg Academy of Sciences.
- Taught at various institutions in Saint Petersburg:
  - 1836-1860 Military Engineering-Technical University
  - 1831-1862 Institute of Railway Engineers
  - 1828-1860 Naval Cadet Corps
  - 0 1832-1861 Main Pedagogical Institute
  - o 1841-1860 Mikhailovsky Artillery School
- Notable works:
  - Lectures on algebraic and transcendental analysis (1857).
  - Selected works (1958).



#### M. Ostrogradsky, Mem. Ac. St. Petersburg 6, 385 (1850)

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 $H = P_1 Q_2 + P_2 f(Q_1, Q_2, P_2) - L(Q_1, Q_2, P_2).$ 

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# Hamiltonian is linear in  $P_1 \Rightarrow$  Energy is not bounded from below.

# Lev Landau

- \* January 22, 1908, Baku; † April 1, 1968, Moscow.
- 1920 graduated from gymnasium.
- 1920-1922 studied at Baku Economical Technicum.
- 1922-1924 studied chemistry and physics at Baku University.
- 1924-1927 continued studies at Leningrad State University.
- 1927-1934 post-graduate, Leningrad Physico-Technical Institute.
- 1929-1931 visited Copenhagen and other European cities.
- 1932-1937 head of Department of Theoretical Physics, Kharkiv Institute of Physics.
- 1932-1936 taught at Institute for Mechanical Engineering (now Polytechnic Institute).
- 1934 established "Landau school", created "Theoretical Minimum".
- 1935 taught physics at Kharkiv University, awarded degree of Professor.
- 1937-1962 head of Theoretical Division, Institute for Physical Problems, Moscow.
- 1938-1939 arrested for publishing anti-Stalinist flyer.
- 1962 Nobel prize (physics) "For pioneer investigations in the theory of condensed matter and especially of liquid helium"





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• L. Landau, On the theory of phase transitions, Zh. Eksp. Theor. Fiz. 7, 19 (1937).

# Evgeny Lifshitz

- \* February 21, 1915, Kharkiv; † October 29, 1985, Moscow.
- Mostly educated at home, only 6th-7th grade at school.
- Completed secondary school in 1929 at the age of 14.
- 1929-1931 studied at chemical college.
- 1931-1933 Mechanics and Machine Building Institute.
- 1933 passed Landau's "Theoretical Minimum".
- 1933-1934 PhD at Institute of Physics and Technology.
- 1934-1938 senior research scientist at Inst. Phys. Tech.
- 1939 D.Sc. at Leningrad State University.
- Since 1939 worked at Inst. of Physical Problems, Moscow.



- State Prize of USSR 1954, Lomonosov Prize 1958, Lenin Prize 1962 with L. Landau, Landau Prize 1974.
- Since 1966 corresponding member, since 1979 full member of the Academy of Sciences of the USSR.

Landau, L.D.; Lifshitz, E.M. (1935). "Theory of the dispersion of magnetic permeability in ferromagnetic bodies". Phys. Z. Sowjetunion. 8, 153.

The distribution of magnetic moments in a ferromagnetic crystal is investigated. It is found that such a crystal consists of elementary layers magnetized to saturation. The width of these layers is determined. In an external magnetic field, the boundaries between these layers move; the velocity of this propagation is determined. The magnetic permeability in a periodical field parallel and perpendicular to the axis of easiest magnetization is found.

- Magnetization  $\vec{M}$  in ferromagnet equals saturation:  $|\vec{M}| = M_s$ .
- Direction of magnetization follows Landau-Lifshitz equation:

$$\frac{d\vec{M}}{dt} = -\gamma \vec{M} \times \vec{H}_{\text{eff}} - \lambda \vec{M} \times (\vec{M} \times \vec{H}_{\text{eff}}) \,.$$

- $\circ \gamma$ : electron gyromagnetic ratio.
- $\circ~\lambda$  : phenomenological damping parameter.
- $\vec{H}_{eff}$ : effective field composed of external field and material effects.

# Course of theoretical physics

- Comprehensive textbook in 10 volumes:
  - I. Mechanics
  - II. The Classical Theory of Fields
  - III. Quantum Mechanics: Non-Relativistic Theory
  - IV. Relativistic Quantum Theory (later: Quantum Electrodynamics)
  - V. Statistical Physics
  - VI. Fluid Mechanics
  - VII. Theory of Elasticity
  - VIII. Electrodynamics of Continuous Media
  - IX. Statistical Physics, Part 2: Theory of the Condensed State
  - X. Physical Kinetics



<sup>1</sup>Matvei Petrovich Bronstein, \* November 29, 1906, Vinnytsia; † February 18, 1938, Leningrad.

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  - Mechanics, Statistics, Electrodynamics by Landau, Piatigorsky and Lifshitz 1935-1938.

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  - Translated to English, German, French, Italian and other languages.
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Kharkiv's role in theoretical physics





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• Helpful to determine emitted gravitational waves by perturbative expansion.

- \* May 13, 1949, Kharkiv.
- 1966-1971 studied physics at Kharkiv University.
- Turned down offer to work for KGB; was denied PhD studies.
- Drafted to building brigade.
- Worked at zoo in Kharkiv as night watchman.
- Emigrated to USA with wife and daughter in 1976.
- 1976-1977 PhD at Buffalo State University of New York.
- 1978 Visiting Assistant Professor, Tufts University.
- 1979 Assistant Professor, Tufts University.
- 1983 Associate Professor, Tufts University.
- 1987 Professor, Tufts University.
- Wrote more that 260 articles on cosmology and two books:
  - A. Vilenkin, E. P. S. Shellard: Cosmic Strings and Other Topological Defects (2000).
  - A. Vilenkin: Many Worlds in One: The Search for Other Universes (2007).



### Eternal inflation and the multiverse

- The flatness and horizon problems in cosmology:
  - $\circ~$  Observations show that the universe expand  $\Rightarrow$  Big Bang theory.
  - Cosmic microwave background: same temperature at causally disconnected regions?
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- Can inflation be eternal?
  - Phase transition not simultaneous everywhere: "universe bubbles" emerge & expand.
  - Even if bubbles expand at speed of light, exponential expansion dominates.
  - Expanding bubbles are causally disconnected: separate universes in multiverse.
  - Inflation may be eternal in both past and future.

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  - § Spatial geometry of the universe is nearly flat fine tuning of initial conditions?
- Theory of inflation:
  - Universe was expanding exponentially near its beginning until phase transition.
  - $\Rightarrow$  Observed regions of microwave background were connected in the past.
  - $\Rightarrow$  Spatial curvature flattens out during exponential expansion.
- Can inflation be eternal?
  - Phase transition not simultaneous everywhere: "universe bubbles" emerge & expand.
  - $\circ~$  Even if bubbles expand at speed of light, exponential expansion dominates.
  - Expanding bubbles are causally disconnected: separate universes in multiverse.
  - Inflation may be eternal in both past and future.
- Vilenkin's main contributions to eternal inflation:
  - Creating of inflating universe from quantum vacuum ("nothing") [Vilenkin '82].
  - Eternal inflation & multiverse are generic for inflation theories [Vilenkin '83].
  - Inflation cannot be past-eternal, but must have beginning [Borde, Guth, Vilenkin '03].

## Otto Struve

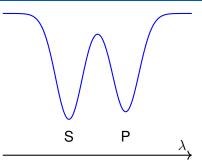
- \* August 12, 1897, Kharkiv; † April 6, 1963, Berkeley.
- Great-grandson of Friedrich Georg Wilhelm von Struve.
- Entered Kharkiv University in 1915 for one semester.
- Enlisted to military artillery school in St. Petersburg 1916.
- Sent to Turkish front in 1917.
- Returned to Kharkiv 1918 and finished studies 1919.
- 1920 escaped from Bolsheviks to Sevastopol, then Turkey.
- 1921 emigrated to USA to work at Yerkes Observatory.
- 1923 defended PhD at University of Chicago.
- 1924 Instructor, University of Chicago.
- 1927 Assistant Professor, University of Chicago.
- 1932 Professor, University of Chicago.
- 1932-1947 Head of Yerkes Observatory.
- 1939-1959 Founding Director of McDonald Observatory.
- 1952-1962 Director of National Radio Astronomy Observatory (Virginia).
- Published more than 900 journal articles and books<sup>2</sup>.

<sup>2</sup>Probably only Estonian astronomer Ernst Öpik, who published 1094 items, published even more.





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  - Absorption lines of both components visible.
  - Spectral lines shift during orbit due to Doppler effect.



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- Gas stream trailing behind secondary star [Struve '50].
- Gas stream from primary to secondary star [Sahade '59].
- Shock of stellar winds displaced by Coriolis force [Gies '97].

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