

**Michael Backes**

**Saarland University, Germany**

**joint work with Birgit Pfitzmann and Michael Waidner**

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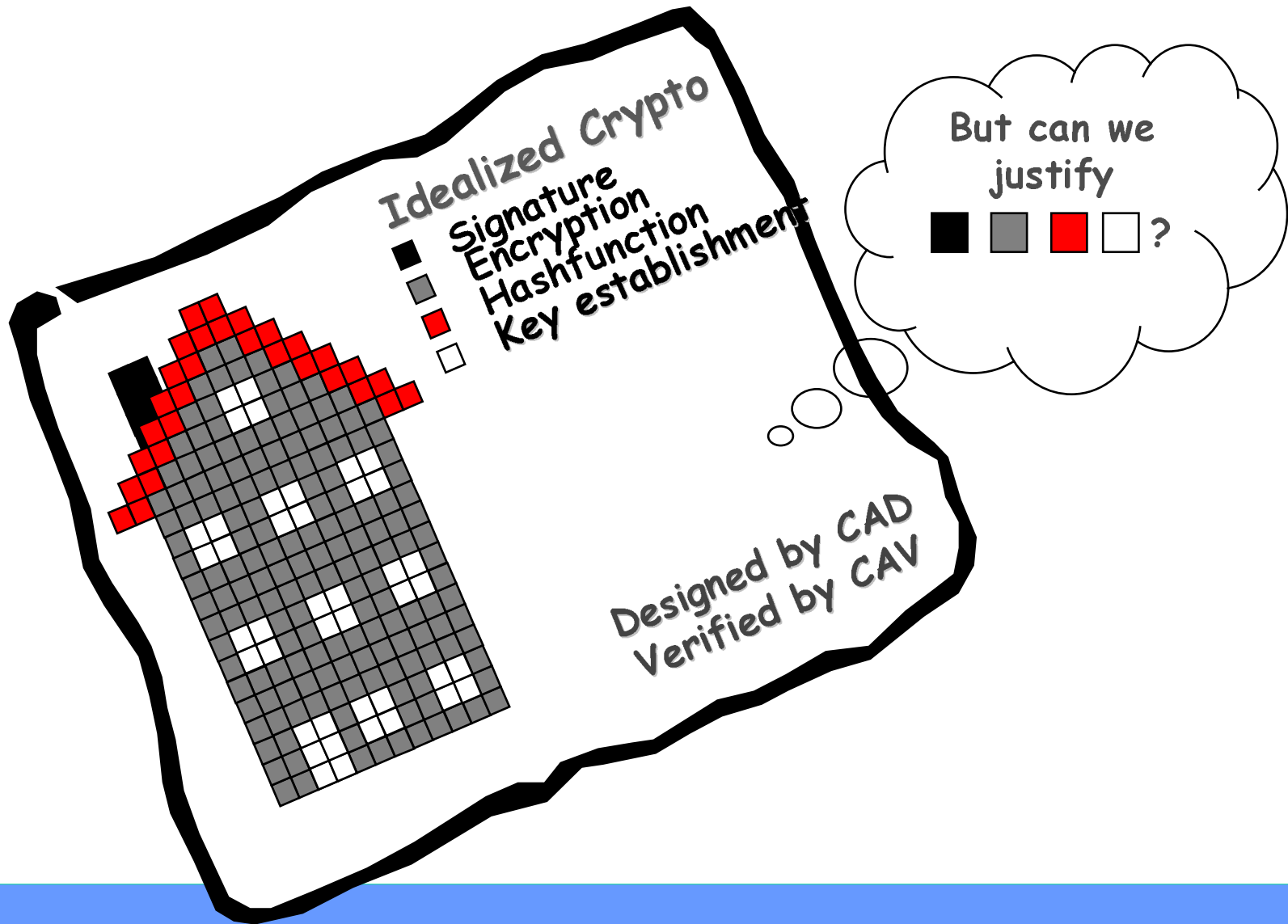
**Secure Reactive Systems, Day 2:**

**Reactive Simulatability –  
Composition and First Applications**

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**Tartu, 02/28/06**

# Recall the Big Picture



# Recall the RS Framework

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- **Precise system model allowing cryptographic and abstract operations**
- **Reactive simulatability** with composition theorem
- Preservation theorems for security properties
- Concrete pairs of idealizations and secure realizations
- Sound symbolic abstractions (Dolev-Yao models) that are suitable for tool support
- Sound security proofs of security protocols: NSL, Otway-Rees, iKP, etc.
- Detailed Proofs (Poly-time, cryptographic bisimulations with static information flow analysis, ... )

# Recall the RS Framework

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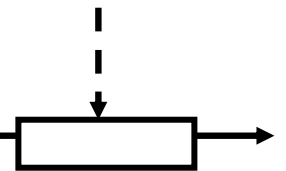
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# Definitions Bottom-up

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## 1. General Model:

- **Collections of probabilistic I/O automata**
  - connections via “ports”
- **Turing machine realization (realistic)**
- **Timing**
  - **Asynchronous: Distributed scheduling via clock ports**
  - **Synchronous: Clk: Subrounds  $\rightarrow P(M^*)$**

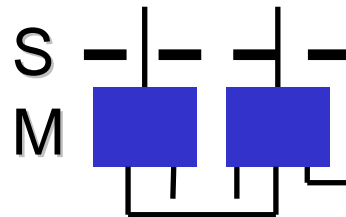


# Definitions Bottom-up

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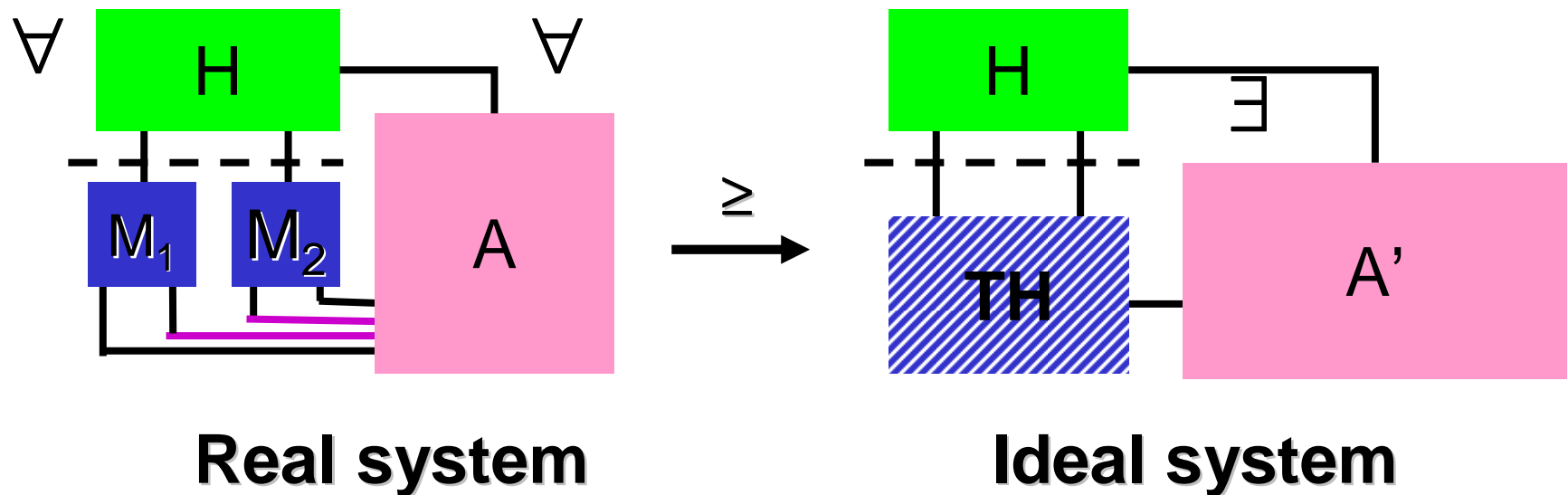
## 2. Security-Specific System Model:

- **Structure:  $(M, S)$  with  $S \subseteq \text{Ports}(M)$**   
“service ports”



- **Configurations:  $(M, S, H, A)$**

# Soundness: Reactive Simulatability



$$\text{view}_{\text{real}}(H) \approx \text{view}_{\text{ideal}}(H)$$

Indistinguishability of  
random variables

# Indistinguishability [Yao\_82]

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**Families of random variables:**

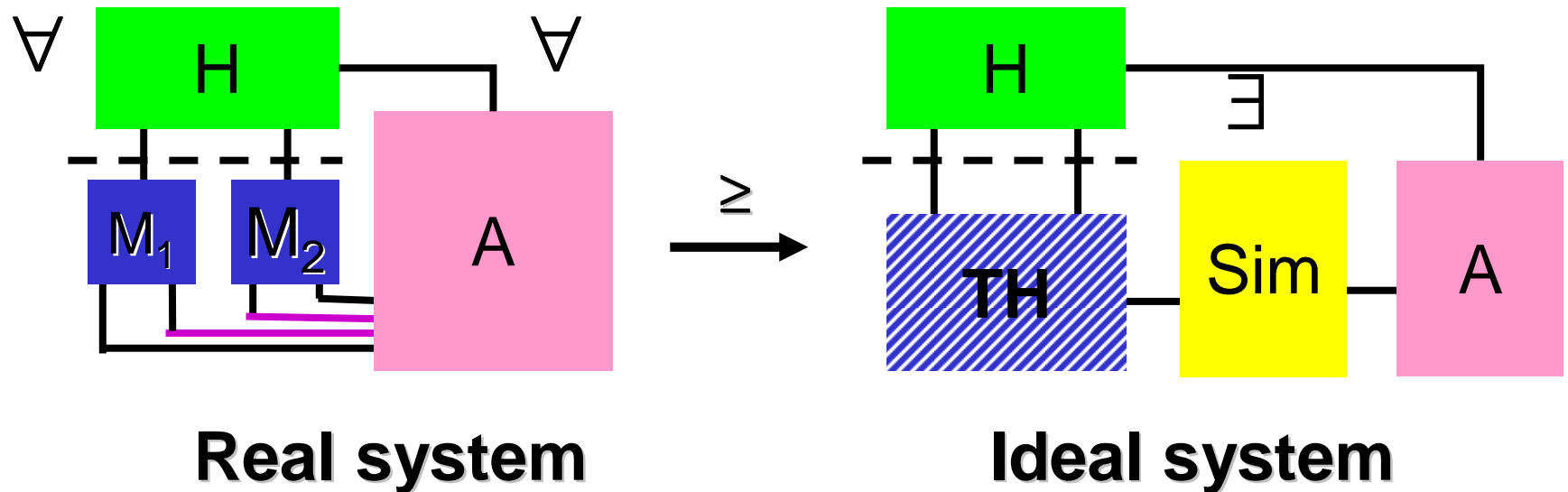
$$(v_k)_{k \in \mathbb{N}} \approx_{\text{poly}} (v'_k)_{k \in \mathbb{N}}$$

$\Leftrightarrow \forall D$  (prob. poly. in first input):

$$\left| \Pr(D(1^k, v_k) = 1) - \Pr(D(1^k, v'_k) = 1) \right| \leq 1 / \text{poly}(k).$$



# Blackbox Reactive Simulatability



$$\text{view}_{\text{real}}(\mathbf{H}) \approx \text{view}_{\text{ideal}}(\mathbf{H})$$

**Sufficient for black-box:**

**M<sub>1</sub>+M<sub>2</sub> behave the same as TH+Sim**

# Some Simple Simulations

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- **On the board...**

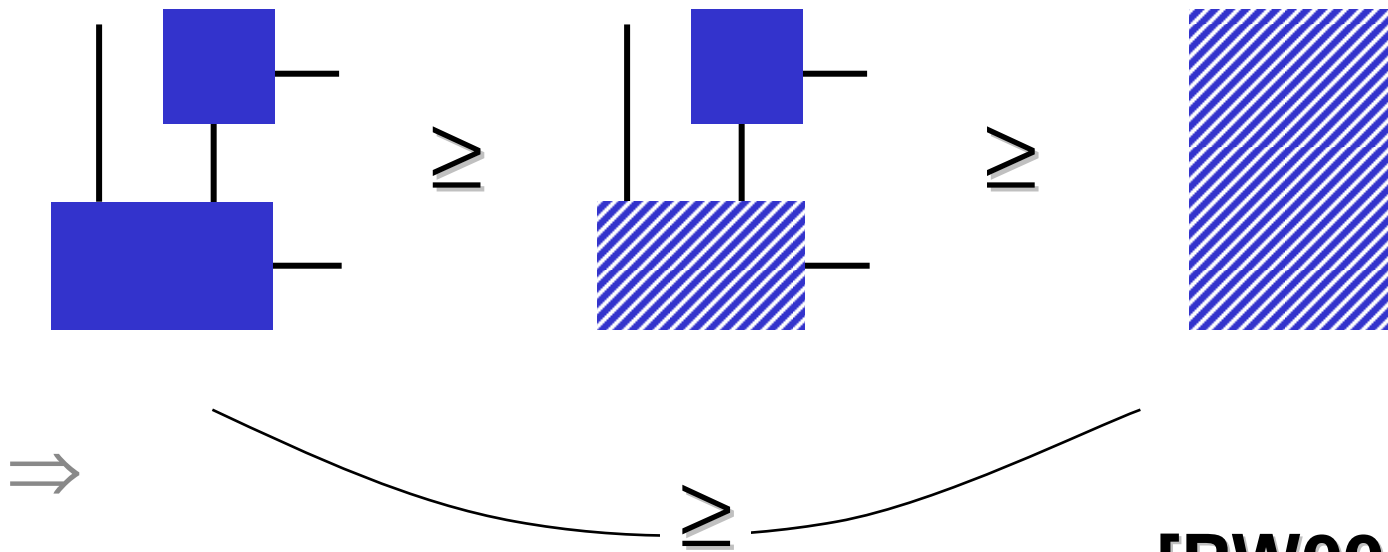
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# Base Lemmas about Reactive Simulatability

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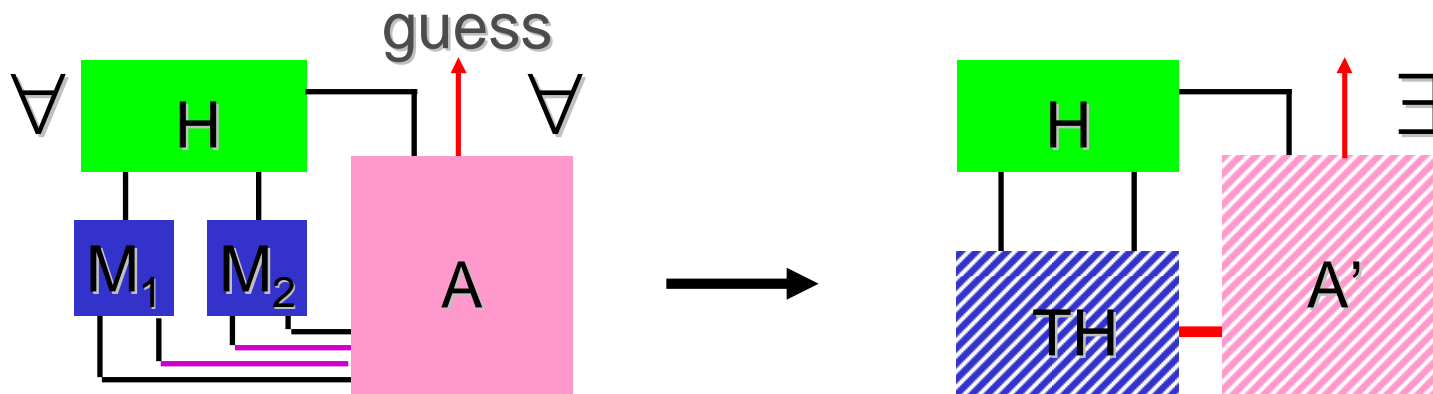
# Base Lemmas (Examples)

- **Machine combination is defined and**
  - is associative
  - retains poly-time (for strong version)
  - retains sub-machine views
- **“As secure as” is transitive. E.g., with composition:**



[PW00,PW01]

# Reactive Simulatability Variants



- Equivalent with “guess”
- Standard simulatability:  $\forall A \forall H \exists A'$
- Universal simulatability:  $\forall A \exists A' \forall H$
- Blackbox simulatability:  $\exists \text{Sim} \forall H \forall A A' = \text{Sim} \& A$
- Perfect / statistic / computational

# Some Other Model Variants

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- **Quantifier order [PSW00,L03,DKMRS04]**
- **Guessing output of adversary [PSW00]**
- **Different types of timing [PSW00,B03]**
- **Different use of “service ports” ( $\approx$  environments) [PSW00]**
- **Auxiliary inputs or not [PSW00]**
- **Mapping of LMMS,PW,C: [DKMRS04, A...04]**
- **Secure, insecure, authentic, reliable, broadcast channels [PSW00,BPSW02]**
- **Static and adaptive corruptions [PW01,C01]**
- **Proactive [BCS03]**

# Composition – One System

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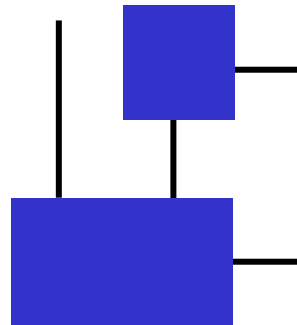
**Given:**



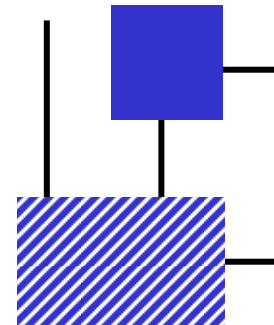
$\equiv$



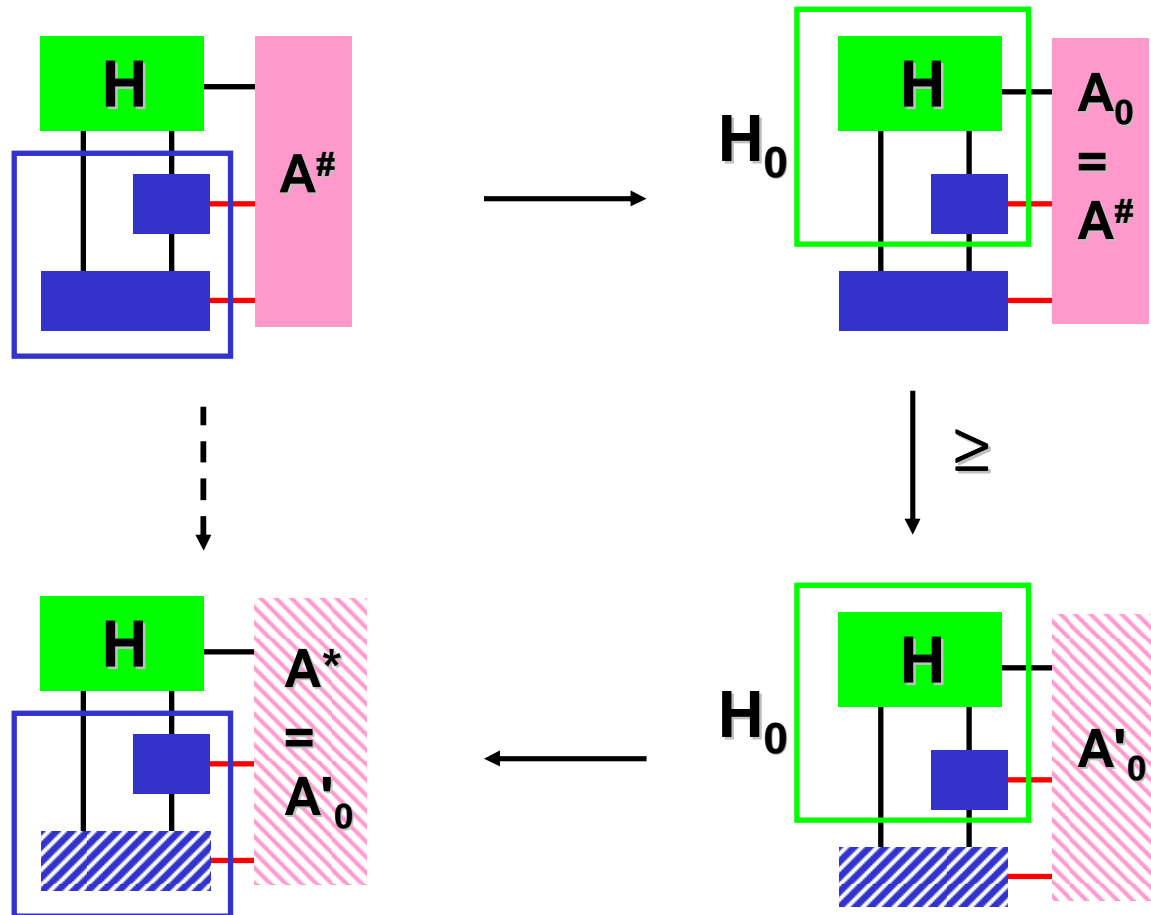
**Then this holds:**



$\equiv$



# Proof Idea (Single Composition)

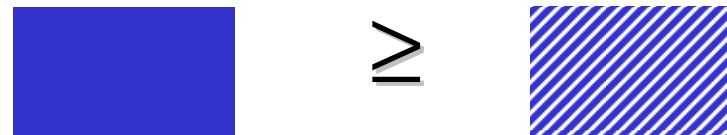




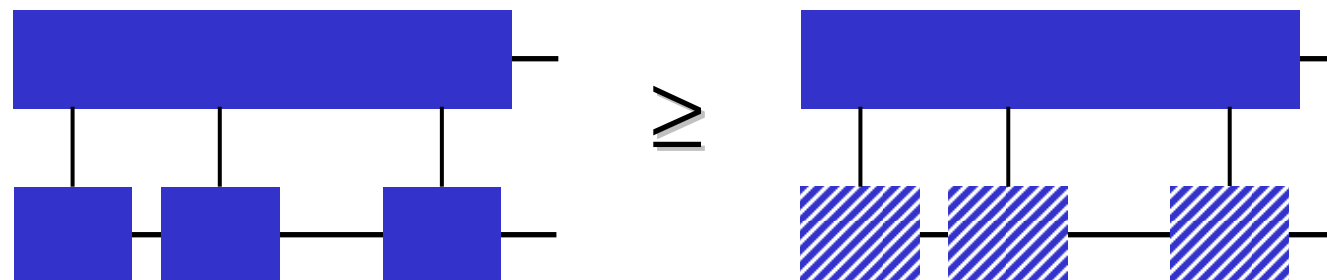
# Composition – Multiple Systems

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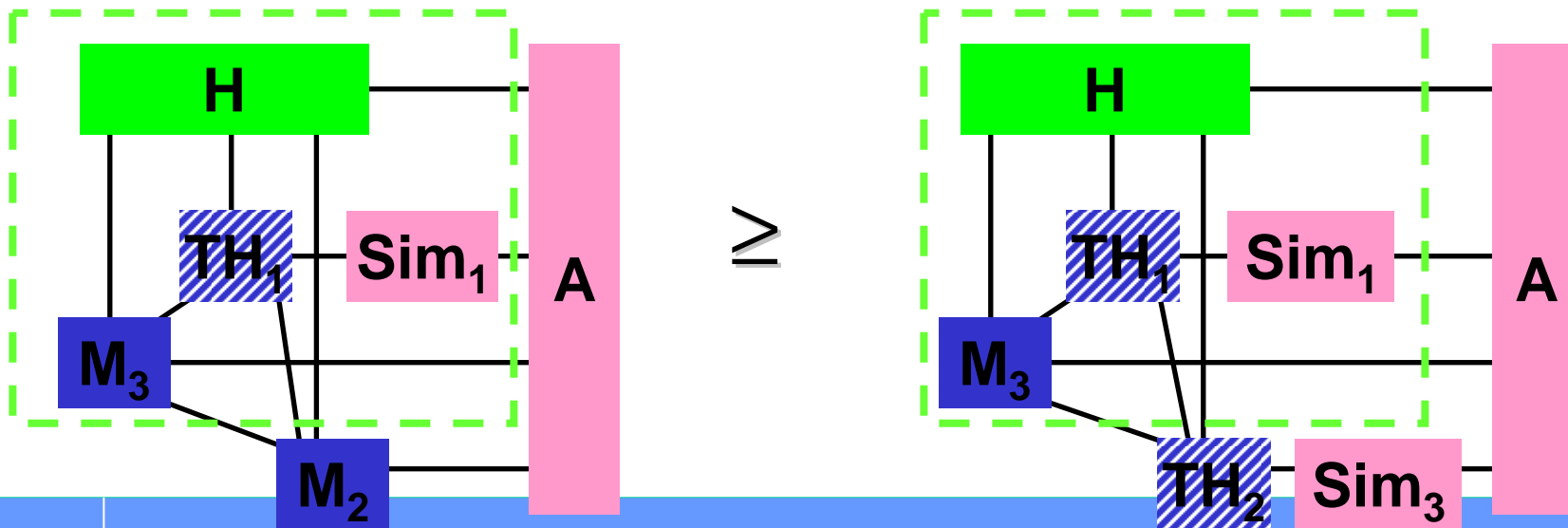
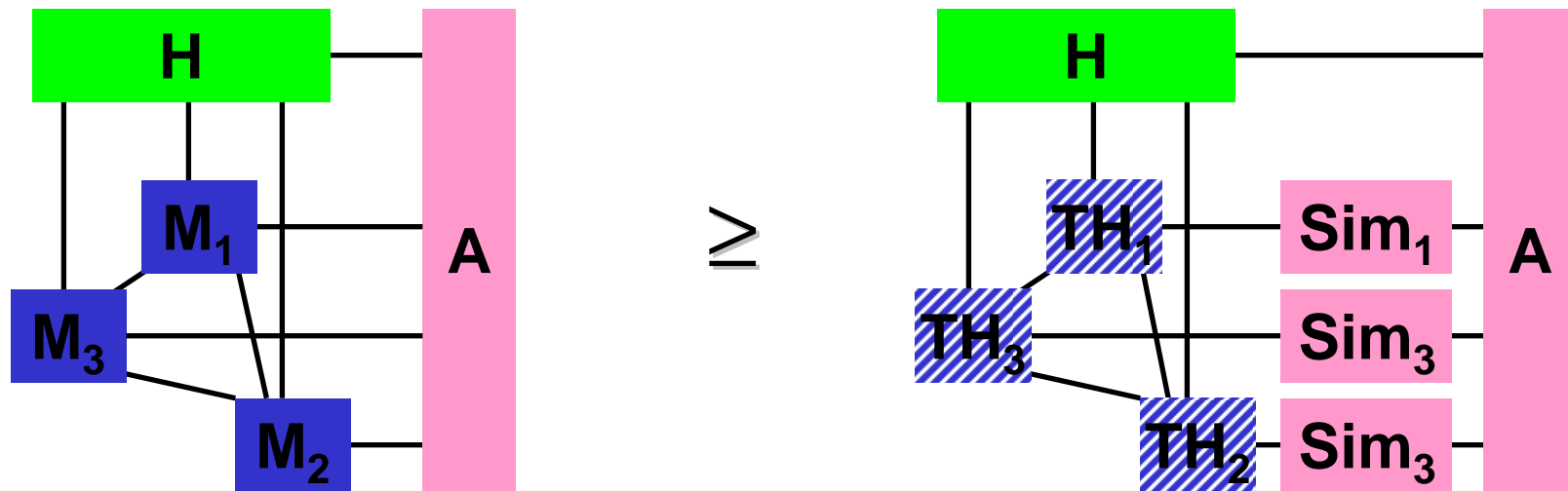
**Given:**



**Also this holds:**



# General Composition Proof via Hybrid Systems



# Composability Types

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	<b>Constant many identical prot.</b>	<b>Constant many different prot.</b>	<b>Poly many identical prot.</b>	<b>Poly many different prot.</b>
<b>General</b>	[PW00, PW01] [L03]	[PW00,PW01] [L03]		
<b>Universal</b>	[PW00, PW01] [C01]	[PW00,PW01]	[C01] [BPW04]	[BPW04]
<b>Blackbox</b>	[PW00, PW01]	[PW00,PW01]	[BPW04]	[BPW04]