

# Meta-analysis: current trends

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# Introduction

Review papers often rely on naming works supporting some hypothesis

If the support is large then the hypothesis is probably true

What about conflicting evidence?



# Introduction (2)

Suppose we can present the research hypothesis as a **null hypothesis test** (i.e. we test whether some effect is zero)

Supporting evidence is then the **papers that have rejected the null hypothesis**



# Introduction (3)

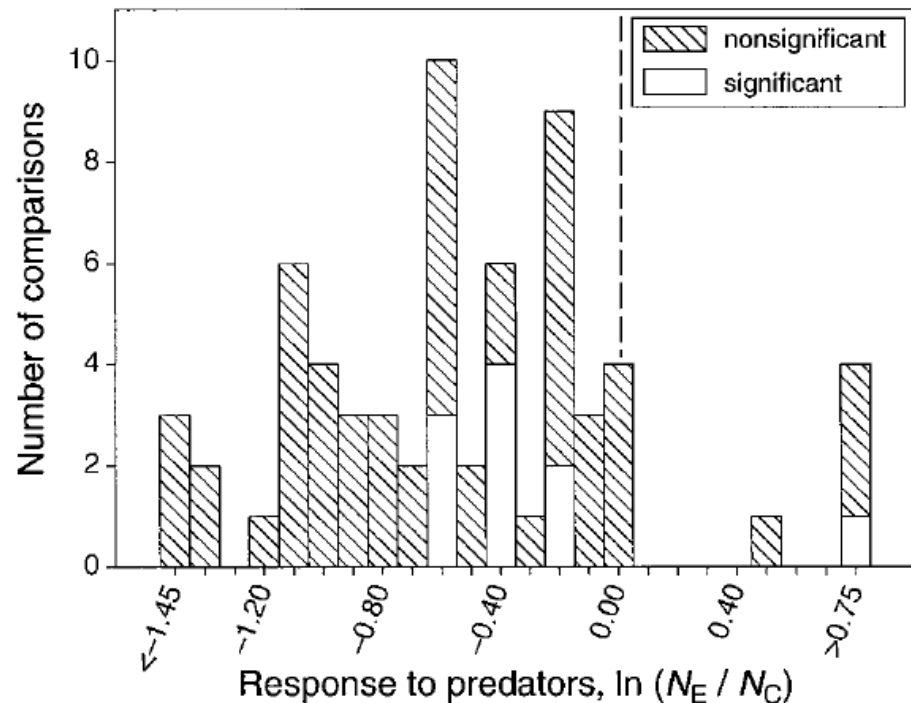
Rejection of the null hypothesis depends on

1. Effect size
2. Sample size
3. Chance

Even if effect size was the same for all studies, sample size varies

# Introduction (4)

Just naming works supporting some hypothesis won't usually tell us anything (meaningful)



From: Osenberg et al. 1999

Resolving ecological questions through meta-analysis: goals, metrics, and models. *Ecology*



# Introduction (5)

Unless all studies have enough power vote-counting is not useful at all

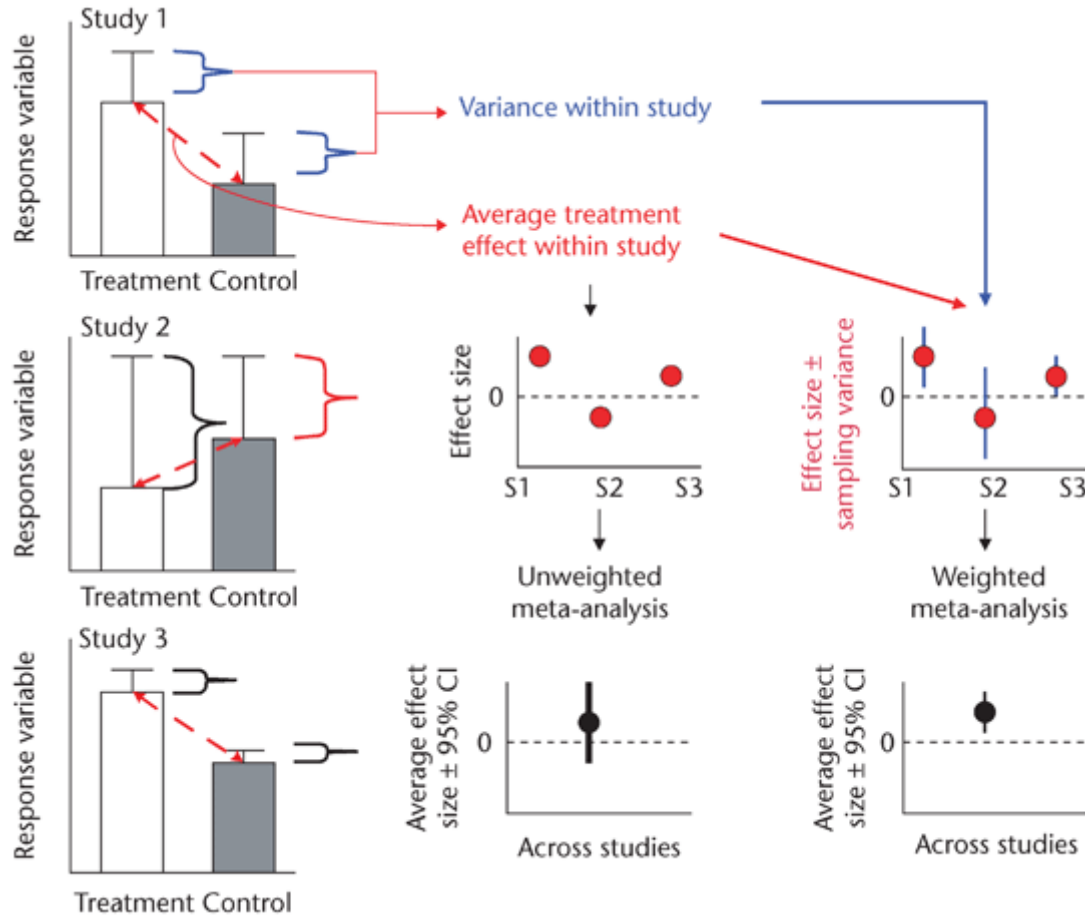
Even if the studies are comparable **is just** the presence of an effect even a question of interest?



# Overview

- General principles
- Current state of the art in meta-analysis
- Challenges
- Tools

# Meta-analysis overview



From: Hillebrand 2008. Meta-analysis in Ecology. *Encyclopedia of Life Sciences*.





# Study compatibility

Studies (however similar) are typically not fully compatible

Study population

Different covariates

Experimental protocol

Time

This means two things

1. We cannot just take parameter estimates
2. Even if we could, the parameter of interest (global mean etc) is not that meaningful

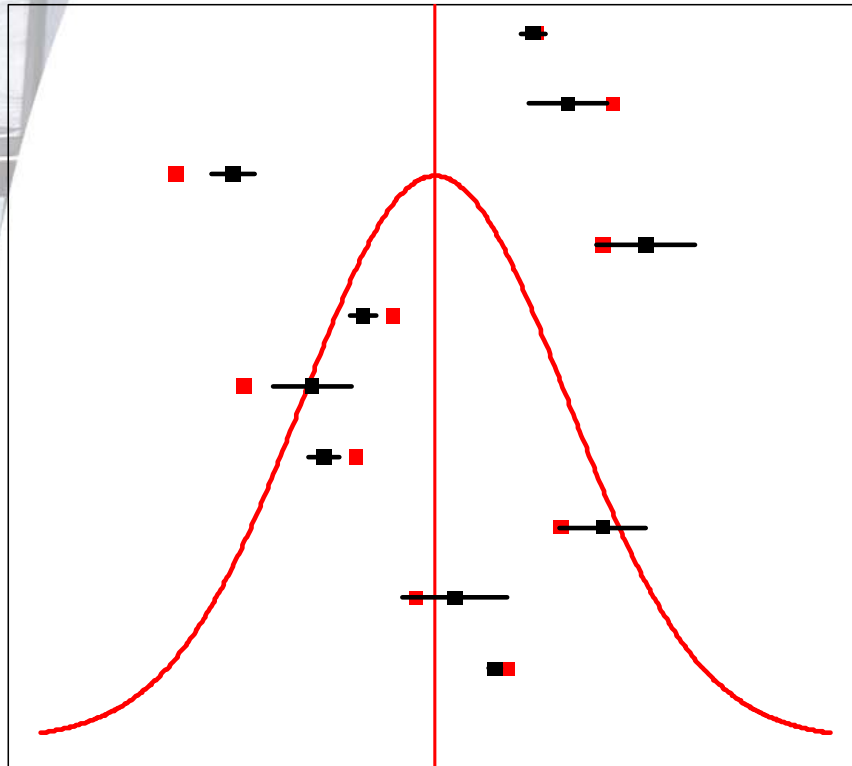
# Standardized effect statistics

The choice depends on the problem but

- continuous-continuous -> correlation
- continuous-dichotomous -> standardized difference in the means
- dichotomous-c/d/other -> odds ratio

Usually **these can be normalized** with a transformation and **standard errors** for the normalized quantities can then be calculated

# Random-Effects meta-analysis model



standardized effects

$$Z_i = \mu + u_i + m_i$$
$$u_i \sim N(0, \sigma_u^2)$$
$$D(m_i) = \sigma_i^2$$

# Meta-regression

Mixed-effects model where covariates are typically at study level

i.e. we try to explain some of the variance between the effects of different studies

$$Z_i = \mu_i + u_i + m_i$$

$$\mu_i = \beta_0 + \sum \beta_i x_i$$

$$u_i \sim N(0, \sigma_u^2)$$

$$D(m_i) = \sigma_i^2$$

# Several effects per study

We should not add study indicator to the fixed effects

So effects from the same study should share a random effect

$$z_i = \mu + u_j + e_i + m_i$$

$$u_j \sim N(0, \sigma_u^2)$$

$$e_i \sim N(0, \sigma_e^2)$$

$$D(m_i) = \sigma_i^2$$



# Several species

We must add additional components to account for the phylogeny

$$z_i = \mu + \mathbf{a}_k + \mathbf{s}_k + u_j + \mathbf{e}_i + m_i$$

$$\mathbf{a} \sim N(\mathbf{0}, \sigma_a^2 \mathbf{A})$$

$$s_k \sim N(0, \sigma_s^2)$$

$u_j, \mathbf{e}_i, m_i$  as before



# Link to comparative analysis

$$z_i = \mu + \mathbf{a}_k + \mathbf{s}_k + u_j + \mathbf{e}_i + m_i$$

$$\mathbf{a} \sim N(\mathbf{0}, \sigma_a^2 \mathbf{A})$$

$$s_k \sim N(0, \sigma_s^2)$$

$u_j, \mathbf{e}_i, m_i$  as before

What if we look at this model from another perspective – we model trait averages



# How complicated is too complicated?

When we cannot estimate the random effects properly then we might take some shortcuts

E.g.

- Phylogenetic correlation at a family level
- Omit some random effects





# Competing models

AIC, DIC are used

general considerations still true e.g.

actual separation between models is  
subjective

AIC is not appropriate when REML is used  
and fixed effects are not the same



# Interpreting the model

Mean of the studied effect is the object of interest

However, we also want to explain the heterogeneity  
(variance components)

Traditionally, Cochran's Q is used

$$Q = \sum \left( \frac{z_j - \hat{\mu}_k}{\sigma_j} \right)^2$$

However, it is quite useless in this context

# Interpreting the model (2)

More useful is the direct use of variance components

$$I^2 = \frac{\sigma_u^2}{\sigma_u^2 + \sigma_m^2}$$

Which can be easily extended as

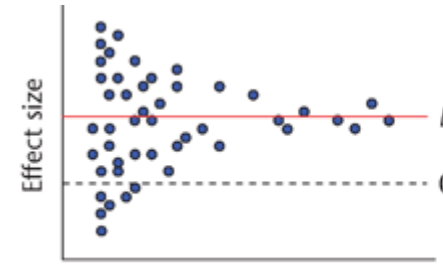
$$I_u^2 = \frac{\sigma_u^2}{\sigma_a^2 + \sigma_s^2 + \sigma_u^2 + \sigma_e^2 + \sigma_m^2}$$



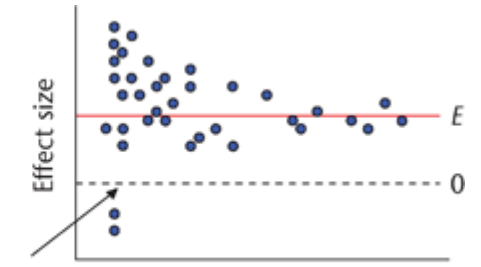
# What can go wrong?

Biased sample of studies

not significant =  
not published



(a) Sample size



(b) Sample size

From: Hillebrand 2008. Meta-analysis in Ecology. *Encyclopedia of Life Sciences.*



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# What can go wrong? (2)

We must still look at the predicted random effects to assess our model

We should not misinterpret the results  
i.e mean might be different from zero but  
actual effect size varies considerably  
across studies



# Detecting publication bias

A basic test is rank correlation between effect size and sampling variance (Begg's test)

Or we could normalize the effects and regress them against sampling variance (Egger's test)

Again problems with heterogeneity



# Detecting publication bias (2)

Possible improvement could be

$$\frac{e_j + m_j}{\sigma_j} = b_0 + b_1 \frac{1}{\sigma_j}$$

where we test the statistical significance of the slope



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# Assessing bias relevancy

Essentially sensitivity analysis

Failsafe calculation – how many studies with no effect to overthrow our conclusion

Trim and fill method – let's restore the symmetric funnel and re-estimate



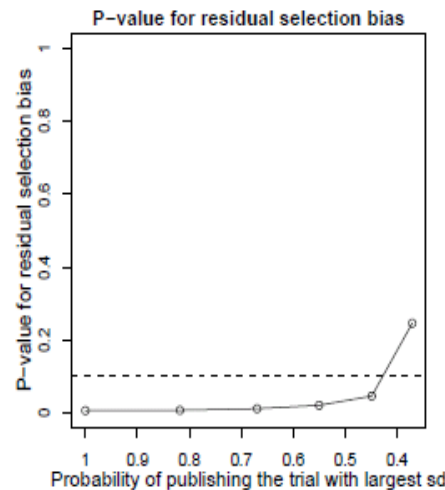
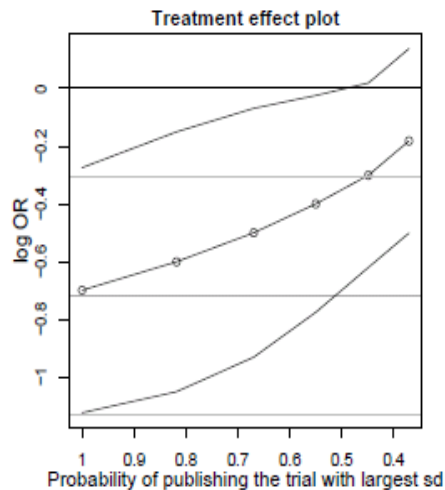
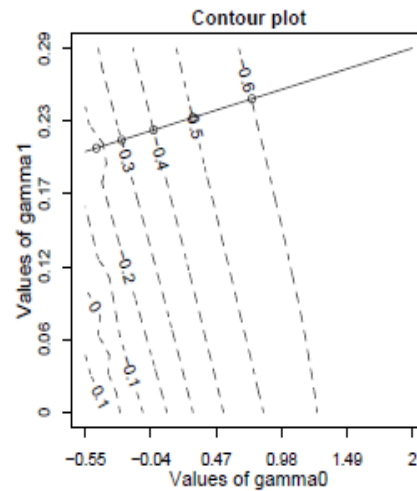
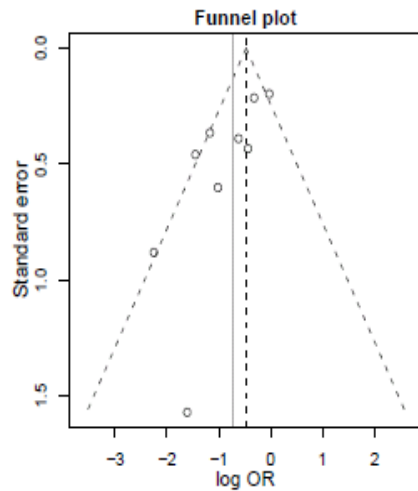
# Assessing bias relevancy (2)

Selection model -- more elaborate approach

We model the correlation between  $u_i + m_i$  and  $\delta_i$ . The latter influence the probability of publication  $\mathbb{P}\{Z > 0\}$ .

$$Z = a + \frac{b}{\sigma_i} + \delta_i, \quad b > 0$$

# Assessing bias relevancy (3)



From:  
Carpenter et al. 2009.  
Copas: an R package for  
fitting the Copas  
selection model.  
*The R journal*



# Tools

Models described are just linear mixed models

Not often easy to fit them with general software (e.g. package lme4 in R)

Often dedicated software is used ([Metawin](#))



## Tools (2)

Things are moving on fast and commercial things just can't keep up

**Metafor** in R is a dedicated state-of-the-art package

Package **MCMCglmm** (in R) can do all that is needed

A former botanist

A mathematician

Meta-analysis is catalyst for  
interdisciplinary work

Thank you  
&  
Questions

First meta-analysis in science (1940)

