

Monaadilised interpretaatorid

- Lihtsa funktsionaalse keele avaldised

```
type Name = String
```

```
data Expr = Var Name  
          | Con Int  
          | Lam Name Expr  
          | App Expr Expr
```

- Väärtused

```
data Value = Num Int  
           | Fun (Value -> M Value)
```

Monaadilised interpretaatorid

- Keskonnad

```
type Env    = [(Name,Value)]
```

```
lookupE :: Name -> Env -> M Value
```

```
lookupE x [] = fail ("Free variable: " ++ x)
```

```
lookupE x ((y,v):e) | x == y = return v  
                    | otherwise = lookupE x e
```

- Interpretaator

```
eval :: Expr -> Env -> M Value
```

```
eval (Var x) env = lookupE x env
```

```
eval (Con i) env = return (Num i)
```

```
eval (Lam x e) env = return (Fun(\a -> eval e ((x,a):env)))
```

```
eval (App h e) env = do Fun f <- eval h env  
                        a      <- eval e env  
                        f a
```

Monaadilised interpretaatorid

- Primitiivsed operaatorid

```
initialE :: Env
initialE = [("+", mkop (+)), ("-", mkop (-)),
            ("*", mkop (*)), ("/", divop)]
  where mkop op = Fun (\(Num a) ->
                        return (Fun (\(Num b) ->
                                      return (Num (a 'op' b)))))
divop    = Fun (\(Num a) ->
                return (Fun (\(Num b) ->
                              if b == 0
                                then fail "Division by zero"
                                else return (Num (a 'div' b)))))
```

Monaadilised interpretaatorid

- Standartne interpretaator

```
newtype Id a = Id a
```

```
instance Monad Id where
```

```
    (Id x) >>= f  = f x
```

```
    return x      = Id x
```

```
type M a = Id a
```

- Veatöötusega interpretaator

```
type M a = Maybe a
```

Monaadilised interpretaatorid

- Olekumonaad

```
newtype S s a = S (s -> (a,s))
```

```
instance Monad (S s) where
```

```
    return x = S (\s -> (x,s))
```

```
    (S f) >>= k = S (\s -> case f s of
```

```
        (x,s') -> case k x of
```

```
            S g -> g s')
```

Monaadilised interpretaatorid

- Olekumonaad (järg)

```
getS :: S s s
```

```
getS = S (\s -> (s,s))
```

```
setS :: s -> S s ()
```

```
setS x = S (\s -> ((),x))
```

```
runS :: S s a -> s -> (a,s)
```

```
runS (S f) s = f s
```

```
tick :: S Int ()
```

```
tick = do s <- getS  
         setS (s+1)
```

Monaadilised interpretaatorid

- Reduktsiooni samme lugev interpretaator

```
type M a = S Int a
```

```
...
```

```
eval (App h e) env = do Fun f <- eval h env  
                        a      <- eval e env  
                        tick  
                        f a
```

- Reduktsiooni samme kasutav interpretaator

```
data Expr = ...  
          | Count
```

```
...
```

```
eval Count      env = do c <- getS  
                        return (Num c)
```

Monaadilised interpretaatorid

- Väljundmonaad

```
newtype O a = O (String,a)
```

```
instance Monad O where
```

```
    return x = O ("",x)
```

```
    (O (s,x)) >>= k = let O (s',y) = k x in O (s++s', y)
```

```
outO :: Show a => a -> O ()
```

```
outO x = O (show x, ())
```

Monaadilised interpretaatorid

- Vahetulemusi väljastav interpretaator

```
type M a = O a
```

```
data Expr = ...
```

```
    | Out Expr
```

```
...
```

```
eval (Out e) env = do v <- eval e env  
    out0 v  
    return v
```

Monaadilised interpretaatorid

- call-by-name interpretaator

```
data Value = Num Int
           | Fun (M Value -> M Value)
```

```
type Env   = [(Name,M Value)]
```

```
lookupE :: Name -> Env -> M Value
```

```
lookupE x [] = fail ("Free variable: " ++ x)
```

```
lookupE x ((y,v):e) | x == y = v
                    | otherwise = lookupE x e
```

```
...
```

```
eval (App e1 e2) env = do Fun f <- eval e1 env
                        f (eval e2 env)
```

Monaadilised interpretaatorid

- call-by-name interpretaator (järg)

```
initialE :: Env
initialE = [("+", mkop (+)), ("-", mkop (-)),
            ("*", mkop (*)), ("/", divop)]
  where mkop op = return (Fun (\x -> do {Num a <- x;
    return (Fun (\y -> do {Num b <- y;
      return (Num (a 'op' b))}})))))
divop    = return (Fun (\x -> do {Num a <- x;
  return (Fun (\y -> do {Num b <- y;
    if b == 0
      then fail "Division by zero"
      else return (Num (a 'div' b))}})))))
```

Monaadid

- Monaadidega seotud funktsioone

```
sequence    :: Monad m => [m a] -> m [a]
sequence    = foldr mcons (return [])
    where mcons p q = p >>= \x -> q >>= \y -> return (x:y)
sequence_   :: Monad m => [m a] -> m ()
sequence_   = foldr (>>) (return ())

mapM        :: Monad m => (a -> m b) -> [a] -> m [b]
mapM f as   = sequence (map f as)

mapM_       :: Monad m => (a -> m b) -> [a] -> m ()
mapM_ f as  = sequence_ (map f as)

(<=<)       :: Monad m => (a -> m b) -> m a -> m b
f <=< x     = x >>= f
```

Monaadid

- Monaadidega seotud klasse

```
class Functor f where
    fmap :: (a -> b) -> f a -> f b
```

```
instance Functor [] where
    fmap = map
```

```
instance Functor Maybe where
    fmap f Nothing    = Nothing
    fmap f (Just x)   = Just (f x)
```

Monaadid

- Monaadidega seotud klasse

```
class (Monad m) => MonadPlus m where
    mzero :: m a
    mplus :: m a -> m a -> m a
```

```
instance MonadPlus Maybe where
    mzero          = Nothing
    Nothing 'mplus' ys = ys
    xs          'mplus' ys = xs
```

```
instance MonadPlus [] where
    mzero = []
    mplus = (++)
```

- Teegis Monad

Monaadid

- Monaadidega seotud funktsioone

```
liftM    :: (Monad m) => (a -> b) -> (m a -> m b)
```

```
liftM f  = \a -> do { a' <- a; return (f a') }
```

```
liftM2   :: (Monad m) => (a -> b -> c) -> (m a -> m b -> m c)
```

```
liftM2 f = \a b -> do { a' <- a; b' <- b; return (f a' b') }
```

```
liftM3   :: (Monad m) => (a -> b -> c -> d) ->
```

```
          (m a -> m b -> m c -> m d)
```

```
liftM3 f = \a b c -> do { a' <- a; b' <- b; c' <- c;  
                        return (f a' b' c') }
```

Monaadid

- Monaadidega seotud funktsioone

`msum :: MonadPlus m => [m a] -> m a`

`msum xs = foldr mplus mzero xs`

`join :: (Monad m) => m (m a) -> m a`

`join x = x >>= id`

`when :: (Monad m) => Bool -> m () -> m ()`

`when p s = if p then s else return ()`

`unless :: (Monad m) => Bool -> m () -> m ()`

`unless p s = when (not p) s`

`ap :: (Monad m) => m (a -> b) -> m a -> m b`

`ap = liftM2 ($)`

Monaadid

- Monaadidega seotud funktsioone

```
guard    :: MonadPlus m => Bool -> m ()  
guard p  =  if p then return () else mzero
```

```
foldM    :: (Monad m) => (a -> b -> m a) -> a -> [b] -> m a  
foldM f a []      = return a  
foldM f a (x:xs) =  f a x >>= \ y -> foldM f y xs
```

```
filterM  :: Monad m => (a -> m Bool) -> [a] -> m [a]  
filterM p []      = return []  
filterM p (x:xs) = do b  <- p x  
                    ys <- filterM p xs  
                    return (if b then (x:ys) else ys)
```